

**BONAM VENKATA CHALAMAYYA INSTITUTE OF TECHNOLOGY &
SCIENCE**

(AUTONOMOUS)

I - B. Tech II-Semester Regular/Supplementary Examinations (BR23), June – 2025
DIFFERENTIAL EQUATIONS & VECTOR CALCULUS (Common to All Branches)

Time: 3 hours

Max. Marks: 70

Question Paper consists of Part-A and Part-B
*Answer ALL the question in **Part-A and Part-B***

PART-A (10X2 = 20M)

	Marks	CO	BL
1. a) Solve $\frac{ydx - xdy}{x^2} + e^y dy = 0$.	(2M)	CO1	L2
b) State Newton's Law of Cooling and write the differential equation of it.	(2M)	CO1	L1
c) Solve $(D^2 + 1)y = 0$.	(2M)	CO2	L2
d) Find the P.I of $(D^2 + 1)y = e^{2x}$.	(2M)	CO2	L2
e) Form the partial differential equation by eliminating the arbitrary function f from $z = f(2x + y)$.	(2M)	CO3	L2
f) Solve the partial differential equation, $p + q = 1$.	(2M)	CO3	L2
g) Find the greatest value of the directional derivative of the function $f = x^2 + y^2 + z^2$ at $(1,1,1)$.	(2M)	CO4	L2
h) Find $\nabla \times \vec{f}$, where $\vec{f} = z\vec{i} + x\vec{j} + y\vec{k}$.	(2M)	CO4	L2
i) If $\vec{F} = ax\vec{i} + by\vec{j} + cz\vec{k}$, where a, b, c are constants then find $\iint_S \vec{F} \cdot \vec{n} \, dS$, where S is the surface of the unit sphere.	(2M)	CO5	L2
j) State Stoke's theorem.	(2M)	CO5	L1

PART-B (5X10 = 50M)

2.a) Solve $\frac{dy}{dx} - \frac{2y}{x+1} = (x+1)^2$.	5(M)	CO1	L3
b) A bacterial culture, growing exponentially, increases from 200 to 500 grams in the period from 6 a.m. to 9 a.m. How many grams will be present at noon. (OR)	5(M)	CO1	L3
3.a) Solve $x^2 y dx - (x^3 + y^3) dy = 0$.	5(M)	CO1	L3
b) If the temperature of a body is changing from 100°C to 70°C in 15 minutes, find when the temperature will be 40°C , if the temperature of air is 30°C .	5(M)	CO1	L3

- 4.a) Solve $(D^2 - 4)y = 2\cos^2 x$. 5(M) CO2 L2
- b) In an electric circuit, inductance(L) = 0.25 Henries, resistance(R) = 250 Ohms, capacitance(C) = 2×10^{-6} Farads, then find the charge q(t). 5(M) CO2 L3
- (OR)
5. Apply the method of variation of parameters to solve $\frac{d^2 y}{dx^2} - 3\frac{dy}{dx} + 2y = \frac{e^x}{1+e^x}$. 10(M) CO2 L3
- 6.a) Form a partial differential equation by eliminating the arbitrary constants h, k from $(x - h)^2 + (y - k)^2 + z^2 = a^2$. 5(M) CO3 L2
- b) Solve the partial differential equation, $(y - z)p + (x - y)q = (z - x)$. 5(M) CO3 L3
- (OR)
- 7.a) Form a partial differential equation by eliminating the arbitrary functions $f(x)$ and $g(y)$ from $z = yf(x) + xg(y)$. 5(M) CO3 L2
- b) Solve the partial differential equation, $(D^3 - 7DD'^2 - 6D'^3)z = e^{2x+y}$. 5(M) CO3 L3
- 8.a) Find the directional derivative of $\phi = x^2 - 2y^2 + 4z^2$ at (1,1, -1) in the direction of $2\bar{i} + \bar{j} - 2\bar{k}$. 5(M) CO4 L2
- b) Find $\text{curl } \bar{f}$, where $\bar{f} = \text{grad}(x^3 + y^3 + z^3 - 3xyz)$. 5(M) CO4 L2
- (OR)
9. Show that vector $(x^2 - yz)\bar{i} + (y^2 - zx)\bar{j} + (z^2 - xy)\bar{k}$ is irrotational and find its scalar potential. 10(M) CO4 L3
- 10.a) Find the line integral $\int (y^2 dx - x^2 dy)$ round the triangle whose vertices are (1,0), (0,1), (-1,0) in the xy -plane. 5(M) CO5 L2
- b) Using Gauss Divergence theorem to evaluate, $\iint [(x + z)dydz + (y + z)dzdx + (x + y)dxdy]$ over S, where S is the surface of the sphere $x^2 + y^2 + z^2 = 4$. 5(M) CO5 L3
- (OR)
11. Verify Green's theorem $\int [(2xy - x^2)dx + (x^2 + y^2)dy]$ over the curve C, where C is the closed region bounded by the curves: $y = x^2$ and $y^2 = x$. 10(M) CO5 L5
